

Find the real root of the Equation: $f(x) = x^3 - 4x - 9 = 0$ by using bisection method/ Bolzano method upto 3 decimal places ?

Solution:

Let,

$$F(x) = x^3 - 4x - 9 = 0$$

Now,

$$\text{Put } x=0:- 0^3 - 4*0 - 9 = -9 \text{ (-ve)}$$

$$\text{Put } x=1:- 1^3 - 4*1 - 9 = -13 \text{ (-ve)}$$

$$\text{Put } x=2:- 2^3 - 4*2 - 9 = -9 \text{ (-ve)}$$

$$\text{Put } x=3:- 3^3 - 4*3 - 9 = 6 \text{ (+ve)}$$

Therefore the roots lie between 2 and 3:

1st stage:-

Hence,

$$x_0 = 2 + \frac{3-2}{2} = \frac{5}{2}$$

$$x_0 = 2.5$$

now,

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$$f(x_0) = 2.5^3 - 4 \cdot 2.5 - 9 = 0$$

$$f(x_0) = -3.375$$

So, the roots lie between x_0 and $2(x_0$ which is 2.5):

2nd stage:-

Hence,

$$x_1 = 2.5 + 3/2 =$$

$$x_1 = 2.75$$

now,

$$f(x_1) = 2.75^3 - 4 \cdot 2.75 - 9$$

$$f(x_1) = 0.796$$

So, the roots lie between x_0 and x_1 (which is 2.5 and 2.75):

3rd stage:-

Hence,

$$x_2 = 2.5 + 2.75/2$$

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$$x_2 = 2.625$$

now,

$$f(x_2) = 2.625^3 - 4 \cdot 2.625 - 9 =$$

$$f(x_2) = -1.412$$

So, the roots lie between x_1 and x_2 (which is 2.75 and 2.625):

4th stage:-

Hence,

$$x_3 = 2.75 + 2.625 / 2 = 2.6875$$

$$x_3 = 2.6875$$

now,

$$f(x_3) = 2.6875^3 - 4 \cdot 2.6875 - 9 =$$

$$f(x_3) = -0.347$$

here, the roots lie between x_1 and x_3 :

5th stage:-

Find the real root of the Equation: $f(x) = x^3 - 4x - 9 = 0$ by using bisection method/ Bolzano method upto 3 decimal places ?

Hence,

$$x_4 = \frac{2.75 + 2.06875}{2}$$

$$x_4 = 2.718$$

now,

$$f(x_4) = 2.718^3 - 4 \cdot 2.718 - 9 =$$

$$f(x_4) = 0.207$$

here, the roots lie between x_1 and x_3 :

6th stage:-

Hence,

$$x_5 = \frac{2.6875 + 2.718}{2}$$

$$x_5 = 2.702$$

now,

$$f(x_5) = 2.702^3 - 4 \cdot 2.702 - 9 =$$

$$f(x_5) = -0.081$$

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here, the roots lie between x_4 and x_5 :

7th stage:-

Hence,

$$x_6 = \frac{2.702 + 2.718}{2}$$

$$x_6 = 2.71$$

now,

$$f(x_6) = 2.71^3 - 4 \cdot 2.71 - 9 =$$

$$f(x_6) = 0.062$$

here, the roots lie between x_5 and x_6 :

8th stage:-

Hence,

$$x_7 = \frac{2.702 + 2.71}{2}$$

$$x_7 = 2.706$$

now,

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$$f(x_7) = 2.706^3 - 4 \cdot 2.706 - 9 =$$

$$f(x_7) = -0.009$$

here, the roots lie between x_5 and x_7 :

9th stage:-

Hence,

$$x_8 = 2.702 + 2.706/2$$

$$x_8 = 2.706$$

now,

$$f(x_8) = 2.706^3 - 4 \cdot 2.706 - 9 =$$

$$f(x_8) = -0.009$$

Hence, the roots lie between $x_8 = 2.706$ upto three decimal number.

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