

Find a real root of the equation $x = e^{-x}$ using newton Raphson method.(R.G.P.V May 2019)

Solution

Let,

$$F(x) = x - e^{-x}$$

$$\text{Now put } x=0: 0 - e^{-0} = -1$$

$$\text{Now put } x=1: 1 - e^{-1} = 0.6321$$

Thus the roots lie between 0 and 1.

Then,

$$x_0 = 0+1/2 = 0.5$$

$$x_0 = 0.5$$

By Newton Raphson Formula:

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

Here from given equation $f(x_n) = x - e^{-x}$, $f'(x_n) = 1 + e^{-x}$

So,

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

Now put $n=0$;

$$x_0+1 = x_0 - \frac{x_0 - e^{-x_0}}{1 + e^{-x_0}}$$

Now put the value of $x_0 = 0.5$

$$x_1 = 0.5 - \frac{0.5 - e^{-0.5}}{1 + e^{-0.5}}$$

$$x_1 = 0.5 - \frac{0.5 - 0.60653}{1 + 0.60653}$$

$$x_1 = 0.5 - \frac{-0.10653}{1.60653}$$

$$x_1 = 0.56631$$

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

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Now put n=1;

$$X_1+1 = X_1 - X_1 - e^{-X_1} / 1 + e^{-X_1}$$

Now put the value of $X_1 = 0.56631$

$$X_2 = 0.56631 - 0.56631 - e^{-0.56631} / 1 + e^{-0.56631}$$

$$X_2 = 0.56631 - (-0.001306) / 1.567616$$

$$X_2 = 0.56714$$

$$X_{n+1} = X_n - f(X_n) / f'(X_n)$$

Now put n=2;

$$X_2+1 = X_2 - X_2 - e^{-X_2} / 1 + e^{-X_2}$$

Now put the value of $X_2 = 0.56714$

$$X_3 = 0.56714 - (-0.56714) - e^{-0.56714} / 1 + e^{-0.56714}$$

$$X_3 = 0.56714 - (-0.00000516) / 1.56714$$

$$X_3 = 0.56714.$$

Hence, the required root is 0.56714

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