

By using Newton Raphson Method, $x^4-x-10=0$ which is nearest to 2, find real root correct to three decimal places? (R.G.P.V. 2022 NOV)

Solution:

Let,

$$F(x) = x^4 - x - 10$$

Newton Raphson Formula:
 $X_{n+1} = X_n - f(X_n)/f'(X_n)$

Here,

$$f'(X_n) = 4x^3 - 1$$

According to the question, it will be given $x_0 = 2$.

$$X_{0+1} = x_0 - (x_0^4 - x_0 - 10)/(4x_0^3 - 1)$$

$$X_1 = x_0 - (x_0^4 - x_0 - 10)/(4x_0^3 - 1)$$

Put the value of $x_0 = 2$;

$$X_1 = 2 - (2^4 - 2 - 10)/(4 \cdot 2^3 - 1)$$

$$X_1 = 2 - (16 - 12)/4 \cdot 8 - 1$$

$$X_1 = 2 - 4/13$$

$$X_1 = 1.871$$

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Here $x_1 = 1.871$, and $n=1$

$$X_{n+1} = X_n - \frac{(X_n^4 - X_n - 10)}{(4X_n^3 - 1)}$$

Put the value of $n=1$

$$X_{1+1} = X_1 - \frac{(X_1^4 - X_1 - 10)}{(4X_1^3 - 1)}$$

Put the value of $x_1 = 1.871$

$$X_2 = 1.871 - \frac{(1.871^4 - 1.871 - 10)}{(4 \cdot 1.871^3 - 1)}$$

$$X_2 = 1.856$$

Here, $x_2 = 1.856$, and $n = 2$

$$X_{n+1} = X_n - \frac{(X_n^4 - X_n - 10)}{(4X_n^3 - 1)}$$

Put $n = 2$

$$X_{2+1} = X_2 - \frac{(X_2^4 - X_2 - 10)}{(4X_2^3 - 1)}$$

Put the value of $x_2 = 1.856$

$$X_3 = 1.856 - \frac{(1.856^4 - 1.856 - 10)}{(4 \cdot 1.856^3 - 1)}$$

$$X_3 = 1.856$$

By using Newton Raphson Method, $x^4-x-10=0$ which is nearest to 2, find real root correct to three decimal places? (R.G.P.V. 2022 NOV)

Since, $x_2=x_3$, so the real root correct to three decimal place is 1.856.

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