

Show that $a*b=b*a$

Let $(\{a, b\}, *)$ be a semigroup where $aa = b$. Show that- $ab=b*a$.

Sol.

Given

$(\{a*b\}, *)$ is a semigroup

And $a*a = b$.

Now

$$ab = a(aa) (\because aa=b)$$

$$ab = (aa)*a \text{ (by associative law)}$$

$$ab = ba (\because a*a=b)$$